

Sharing the Cost of Backbone Networks: Simplicity vs. Precision

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Abstract—Internet backbone operators face a trade-off in quantifying the costs that their customers inflict on their infrastructure since the precision of these methods depends on the resources dedicated to traffic monitoring. Operators prefer simple and straightforward monitoring schemes, which in turn raises the question of: “what is the price of simplicity in monitoring and cost computation?” We address this question by quantifying the costs of customers with real-world data. Our four-week long dataset describes a large operator’s customer traffic patterns over 401 geographically distributed network links. We study the differences of common cost sharing policies compared to an absolutely accurate and fair policy. The cost discrepancy between different methods exceeds 25% in 71% of the examined cases. We reveal the root cause of these discrepancies by analyzing the customer traffic patterns. Moreover, we quantify the impact of the geographically diverse costs of network links. Our results reveal that simplicity comes at a rather high cost in terms of decoupling between computed and real costs.

I. INTRODUCTION

Commercial Internet backbone providers have been faced with a major challenge in accommodating and delivering the ever increasing volume of Internet traffic over the last decade. Such backbone operators offer paid data transfer services to their customers who are in many cases Internet Service Providers (ISPs) themselves. These large customers insert large amounts of traffic in the network thereby inflicting significant maintenance and upgrade costs upon backbone providers. Quantifying these costs is of utmost importance for ensuring smooth operations at the backbone networks as well as offering fair tariffs to different customer networks.

Computing individual cost contributions is, however, far from simple. The complicated nature of determining the costs is a result of an underlying trade-off: precisely measuring the expenditures for each customer requires significant amount of resources. For example, measuring the volume that a customer inserts in a network can be achieved with a simple SNMP counter on each one of the customer’s access link. Computing the 95% percentile rule [24] at each access link is only marginally more complicated since it requires a few more registers for storing the rates during the 5% intervals with the highest rates. However, to derive a fair share of the cost of a shared device on the backbone requires maintaining extensive flow level time-series in order to be able to break down the peak hour traffic among the different customers. This is typically done using NetFlow technology which however comes at a non-trivial purchase and administration cost. In order to dig deeper into this trade-off we quantify the cost

sharing among customers under various policies based on real-world datasets.

The obtained quantification of the costs inflicted by an individual customer depends on at least three aspects:

- on *where* the operator measures the traffic of the customer, *e.g.*, solely on the ingress links or on every single router and interface of the network;
- on *how* the operator shares the cost of the network infrastructure among its customers, *e.g.*, based on the traffic volumes, maximums, 95th percentiles, *etc.*;
- on *what* is the underlying cost structure of the network, *e.g.*, different devices have diverse cost whereas common functions cost differently at different locations [20].

Each aspect impacts the trade-off between precision and amount of resources utilized for monitoring. First, increasing the number of locations where we meter the traffic increases both precision and resource requirements. Second, utilizing more resources allows applying more sophisticated methods to share the costs among the customers. Third, operators determine the costs of the customers more precisely if they consider the exact cost function of each network device.

Let us consider the toy example in Fig. 1 to illustrate the impact of complexity of cost sharing policies on the computed costs of the customers. The small plots along the links denote the traffic patterns of the network’s two customers while the values represents the costs of the links. In the first case, the operator monitors the total traffic volume of each customer solely on the ingress links (A, B, and C). If we share the aggregate cost of the network based on the customers’ traffic volumes (we will introduce the details of this volume–device cost sharing policy in the next section), the cost of customers are \$118.5 and \$101.5. In the second case, the operator distributes the cost of the network proportionally to the customers’ contribution to the peak utilization of the ingress links (later we refer to this method as aggregate peak–device policy). The quantified costs are \$128.3 and \$91.7 in case of the first and the second customers; the peaks of the first customer’s traffic cause the change in the costs. Thirdly, if the operator deploys monitoring tools on all the network links (*e.g.*, to links D, E, and F as well), it can quantify the cost of the customers more accurately. Based on the customers’ contribution to the peak utilizations of the links, their costs are \$126.5 and \$93.5 as the second customer has an additional peak of link F. Finally, if the operator considers the cost differences over all the links that a customer’s traffic

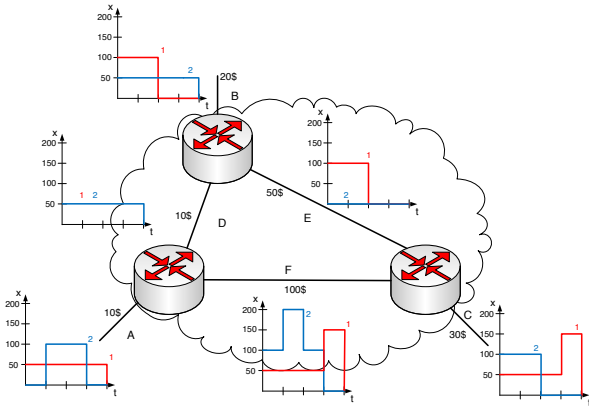


Fig. 1. Toy example: diverse complexity and precision of cost sharing policies. The plots present the traffic volumes of the customers.

traverses, the customers' costs change to \$114.2 and \$105.8 because the second customer utilizes more expensive links. This example shows that the operator captures the costs of customers with more precision if it utilizes more resources to meter the network.

Our work makes the following contributions. First, we quantify the cost of large customers of a backbone operator using real traffic. Specifically, we utilize a four-week long dataset from Netflow traffic information of distinct customers and of 401 geographically distributed network links located in 9 countries. We observe that discrepancies arise among different cost sharing mechanisms; the difference among the costs is more than 25% in 71% of the cases considering the most precise and the simplest methods. Moreover, in 12% of the cases simple pricing is off by at least a factor of $\times 5$. Second, we identify and explain the causes of the discrepancies by analyzing the traffic patterns of customers with the largest discrepancies. The main causes behind the discrepancies are the stepwise cost functions and that the policies do not consider the contribution of individual customers to all the local maxima of the aggregate traffic volumes. Third, we evaluate the impact of differences in the cost structures of network devices due to geographic location. Different parts of a backbone network have diverse costs owed to numerous factors such as energy prices, deployment costs, operational expenses, or taxation. We quantify the impact of cost diversity using real data on transit prices and identify additional discrepancies between the cost policies.

We present our methodology in Section II, where we introduce five policies for network cost sharing and reveal the details of the utilized datasets. In Section III we investigate the discrepancies of the methods based on empirical results. Afterwards, we review the related work in Section IV. Last, in Section V we present the conclusions and outline future research directions.

II. METHODOLOGY

In this section we introduce the details of our methodology, *i.e.*, how we quantify the trade-off between precision and resource needs of the cost sharing policies. We do this by computing the contribution of individual customers to the aggregate cost of the network. To this end, first we introduce

several methods that share the costs of the network devices among the customers. Subsequently, we describe the datasets we use as input parameters.

We quantify the costs of individual customers under the following general setting. A network consists of various network devices, such as routers, switches and links. Let L denote the set of devices of the network and I the set of customers of the network. Let $x_i^l(t)$ denote the traffic volume injected by customer $i \in I$ on network device $l \in L$ during the time interval t in $[1, T]$. Also, let c^l denote the cost of network device l . The cost of a specific device depends on the maximum amount of traffic that it has to carry during a certain time interval. Therefore c^l is obtained by examining the costs of a device for various rates (*e.g.*, 1 Gbps, 10 Gbps, *etc.*) and taking the smallest device whose capacity covers the offered traffic under the requested Service Level Agreement. To this end, we assume that the device costs follow a step function $C: \mathbb{R} \rightarrow \mathbb{R}$. Thus, the cost of device l is

$$c^l = C(\max_{t \in T} \sum_{i \in I} x_i^l(t)) \quad (1)$$

A. Cost Sharing Policies

Next, we present several policies for sharing the aggregate cost of the network infrastructure among the customers. These policies strike different balances between precision and resource needs, which we discuss in more details after their formal descriptions. We note that operators of backbone networks apply some of these policies in practice for pricing purposes like the 95th percentile and the aggregate peak policies. In all cases, we first determine the break down of the cost of a single device among the customers that use it and then sum over all devices to get the total cost inflicted by any given customer.

Volume–device. We measure the amount of data that a single customer sends on the specific network device (*e.g.*, on a single link) for the whole duration of the time-series. Afterwards, we share the cost of the device proportionally to the traffic volumes of the customers using it. Hence, the cost of customer i for device l is:

$$c_i^l = c^l \cdot \frac{\sum_{t \in T} x_i^l(t)}{\sum_{j \in I} \sum_{t \in T} x_j^l(t)} \quad (2)$$

95th percentile–device. We distribute the cost of the device proportional to the 95th percentiles [10] of the customers' traffic that traverses that device. Hence, we quantify the cost of customer i for device l as:

$$c_i^l = c^l \cdot \frac{P_{95}(\dots, x_i^l(t-1), x_i^l(t), x_i^l(t+1), \dots)}{\sum_{j \in I} P_{95}(\dots, x_j^l(t-1), x_j^l(t), x_j^l(t+1), \dots)} \quad (3)$$

where P_{95} denotes the 95th percentile of the arguments.

95th percentile–customer. We utilize this policy in Section III-C to illustrate the importance of the granularity of metering, we study the sharing of the cost of all the network devices based on the 95th percentile of the customer's aggregate traffic. The customer's aggregate traffic can be measured at the entry devices of the network, thus it does not require

metering deep in the network. The total cost of customer i is:

$$c_i = \sum_l c^l \cdot \frac{P_{95}(\dots, \sum_{l \in L} x_i^l(t), \dots)}{\sum_{j \in I} P_{95}(\dots, \sum_{l \in L} x_j^l(t), \dots)} \quad (4)$$

Customer peak–device. Under this policy, we share the expenditure of the network device based on the customers' maximal usage volumes for the given time interval; *i.e.*, the cost of customer i in case of network device l is

$$c_i^l = c^l \cdot \frac{\max_{t \in T} x_i^l(t)}{\sum_{j \in I} \max_{t \in T} x_j^l(t)} \quad (5)$$

Aggregate peak–device. Network operators plan the capacity of the network based on the maximum utilization, *i.e.*, the capacity of a link is larger than the expected maximum of the traffic that traverses it. Accordingly, we distribute the cost of the devices based on the contribution of individual customers to the peak utilization. Assuming that the peak utilization of device l happens at time step $t_m = \arg \max_t \sum_{j \in I} x_j^l(t)$, we allocate the following cost to customer i :

$$c_i^l = c^l \cdot \frac{x_i^l(t_m)}{\sum_{j \in I} x_j^l(t_m)} \quad (6)$$

Shapley–device. This policy distributes the cost of a network device among the customers in a fair way. For example, a small customer starts sending 1 Gbps traffic on a 10 Gbps link that a large customer utilizes nearly completely, *e.g.*, by sending 9.5 Gbps. Due to the traffic of the small customer, the operator has to upgrade the capacity of the link from 10 Gbps to 40 Gbps to handle the elevated traffic volume. The expenditure of the upgrade increases the costs of the network, for which the small customer is mainly responsible. Thus, the fair cost of the small customer is much larger than its share computed solely on the small customer's peak rates. Under this policy, the cost of each customer is proportional to its average marginal contribution to the total cost. Particularly, let us consider all the possible $S \subset I$ subsets (coalitions) of the customers who utilize resources of the network device l . The cost of coalition S depends on the aggregate traffic volume of the participants, *i.e.*, it equals to the cost of a network device having enough capacity:

$$v^l(S) = C(\max_{t \in T} \sum_{j \in S} x_j^l(t)) \quad (7)$$

Based on the v cost function of the coalitions, the $(\phi_1(v), \dots, \phi_N(v))$ Shapley values describe the fair distribution of costs in case of the $S = I$ grand coalition—fair in a way that it satisfies four intuitive fairness criteria [1, 11, 18]. We compute the Shapley value of customer i as

$$\phi_i(v^l) = \frac{1}{N!} \sum_{\Pi \in S_N} (v^l(S(\Pi, i)) - v^l(S(\Pi, i) \setminus i)) \quad (8)$$

where Π is a permutation or arrival order of set N and $S(\Pi, i)$ denotes the set of players who arrived no later than i . Accordingly, we quantify the cost of customer i based on its

Shapley value:

$$c_i^l = c^l \cdot \frac{\phi_i(v^l)}{\sum_{j \in I} \phi_j(v^l)} \quad (9)$$

While we compute the aggregate traffic volumes of the coalitions, we make an assumption. Namely, we assume that *the routing inside the network is static*, *i.e.*, removing some traffic from the network device does not affect the traffic volumes of other customers (*e.g.*, the network does not apply load balancing mechanisms).

Some of the above formulas determine the expenditures caused by the customers on a per device basis. We quantify the aggregate cost of customer i over the whole network as the sum of the costs caused on each network device that his traffic utilizes:

$$c_i = \sum_{l \in L} c_i^l \quad (10)$$

B. Trade-offs of the cost sharing policies

The introduced cost sharing methods make diverse trade-offs in terms of computational complexity, amount of necessary information, and accuracy. We present the policies in an order according to their properties.

Computational resources. The volume–device policy requires the least computational resources as it summarizes only the traffic volumes of the customers. The customer peak–device, the aggregate peak–device, and the 95th percentile–device policies have slightly more complexity because of their maximum and percentile computations. Finally, the Shapley–device method has the largest complexity as it computes the costs based on the different sub-coalitions of the customers. For computational reasons, we consider the 15 largest customer per network device to quantify the costs based on the Shapley–device method. On average, these customers cover 94% of the traffic of the devices.

Necessary information. In terms of the amount of information, all the methods except the Shapley–device policy are similarly modest. They utilize single values for the historical (sum and maximum, respectively) and the current volume or rate values. Contrary, the Shapley–device policy uses the whole time-series of traffic volumes to compute the costs.

Accuracy. The Shapley–device policy method has the highest precision and fairness. The method determines the costs by considering the time when the customers send the traffic, the volume and the burstiness of the traffic, the customers' contribution to the peak utilization as well as the step cost function of the devices. The other policies miss at least one of these resulting lower accuracies. The aggregate peak–device method takes into account the size of the burst and the contribution to the peak utilization of the device, however, it considers only a single point of time. Accordingly, this policy misses the information about how much the customer contributes to the other local maxima of the device's utilization. The 95th percentile–device policy includes the impact of bursts and captures the traffic volumes over multiple time intervals. However, it does not reflect the customers' contribution to the peak utilization and the exact timing of the traffic. The

customer peak–device method solely captures the burstiness of the traffic. Similarly, the volume–device policy focuses exclusively on the aggregate volume of the customers.

C. Datasets

To quantify the costs of the individual customers, we utilize two types of datasets: traffic volumes and cost functions. We collected the time-series of traffic volumes in the network of a backbone provider. We extracted the 95th percentile traffic volumes of individual customers on a two-hour basis using proprietary network monitoring tools. Our dataset contains the traffic information of 401 geographically distributed links located in 9 countries. More specifically, a customer connects to a router through one interface; as the router has multiple interfaces it aggregates the traffic of the customers and forwards this aggregate to the monitoring devices. We select these links because of their number, as they are the leaves of the network, and therefore they account for a large portion of the overall cost of network [3]. The dataset stores 4 weeks of traffic data ranging from 5 May 2011 until 11 June 2011.

As numerous factors impact the network cost, such as hardware costs, energy prices, deployment costs, or taxation—to mention a few—it is challenging to quantify the accurate cost of every single network device. To overcome this issue, we estimate the expenditures of network links based on the wholesale lease prices of a backbone operator. To this extent, we assume that the pricing of the network services is in line with the inferred costs. The cost of network links depends on the capacity of the link, *i.e.*, a link capable to transmit more data costs more. However, the geographic location of the link plays a crucial role in the expenditures. In our empirical study, we apply the normalized prices of network links with different capacities, ranging from E-1 (2 Mbps) throughout STM-4 (622 Mbps) and 2.5G waves to 40G waves (40000 Mbps), and geographic locations such as Europe, USA, and Latin America. The costs of these links define a step function for the network expenditures. Exact values can be provided to interested parties if confidentiality requirements are met.

III. EMPIRICAL RESULTS

In this section we analyze the costs of customers from an empirical point of view by building on the policies and datasets described in the previous section.

A. Discrepancies between the cost sharing policies

First, we focus on the accuracy of the different policies that allocate the cost of the network infrastructure to the customers. In order to focus solely on the features of the methods, we apply the same cost function under all policies.

Network-wide discrepancies: As a starting point, we illustrate in Fig. 2 the discrepancies between the total costs allocated by the investigated policies over all the links using the same cost function. The figure presents the relative costs of those 10 customers whose costs are the largest. We use the largest Shapley–device cost as a reference policy in terms of accuracy and fairness. The plot highlights significant differences between the cost sharing policies. Discrepancies occur regardless of the size of the customers. The real cost of a customer is

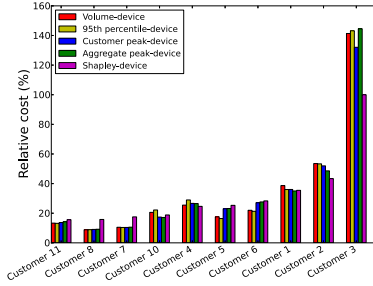


Fig. 2. Aggregated relative costs of the 10 largest customers

quantified by the Shapley–device method, however, none of the other policies reflect the real expenditures accurately.

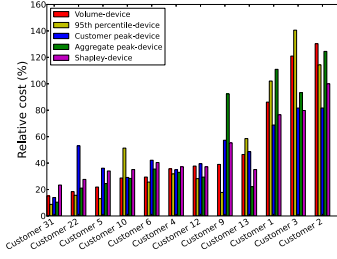
Device-level discrepancies: The dissimilarity of the cost policies also arises when we quantify the costs of the customers in case of individual network links. In Fig. 3(a) we present the relative costs of customers for a link located in the USA. Every policy charges a different cost than the real one on at least on of the 12 customers.

Quantification of the discrepancies: To dive deeper into the relation of the cost sharing policies, we illustrate in Fig. 4 the ratio of the different cost sharing policies and the Shapley–device policy as a function of the percentage of the customers. We consider the ratio of the costs for each customer over all the links in our dataset. The plots confirm our hypothesis that the costs shared based on other allocation policies do not reflect entirely the real cost of a customer, which we quantify based on the Shapley–device policy. A common property of the policies is that they over-, or underestimate the costs of the customers. In particular, the cost of a customer is higher than 125% or lower than 75% of the Shapley costs in 71.48%, 63.82%, 78.47%, and 75.57% of the cases in case of the volume–device, customer peak–device, 95th percentile–device, and the aggregate peak–device policies, respectively. Moreover, the discrepancies occur in the case of non-negligible traffic volumes as we show in the insets of the figures where we weigh the cases with their traffic volumes. Considering the magnitude of the discrepancies, the ratio between the costs is as high as 5 in 11.9%, 4.9%, 21.7%, and 18% of the cases.

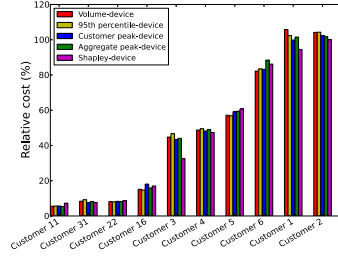
Where do the discrepancies come from: We explore the causes behind these discrepancies by focusing on the traffic patterns of individual customers. In Fig. 5 we present the traffic patterns of customers that have the largest discrepancies in case of non-negligible expenditures, and the aggregate traffic pattern of the other customers utilizing the same link. The differences between the cost sharing policies are causing discrepancies in a way similar to the first and the second case of the toy example. Particularly, the main causes are:

Volume–device policy: The customer is responsible for around half of the traffic flowing on the link (Fig. 5(a)). However, the traffic of the others has huge spikes at the beginning of the fourth week. As the capacity of the link—and thus its cost—is proportional to the largest utilization, these spikes largely contribute to the aggregate cost of the device resulting to modest costs for the investigated customer.

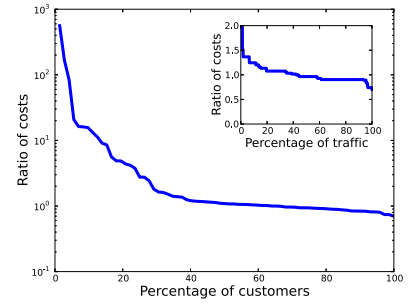
Customer peak–device policy: The bursty traffic of the cus-



(a) In case of a link located in the USA.

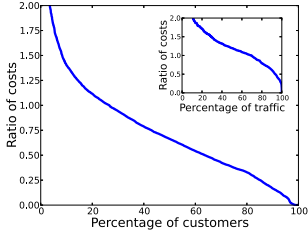


(b) Aggregated relative costs of top 10 customers in case of diverse link expenditures.

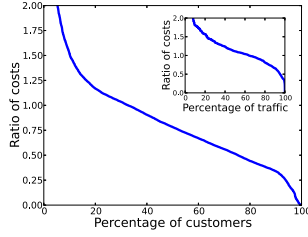


(c) Ratio of the costs of the 95th percentile–device and 95th percentile–customer policies

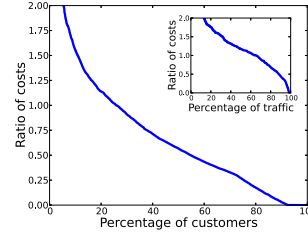
Fig. 3. Discrepancies between the cost sharing policies.



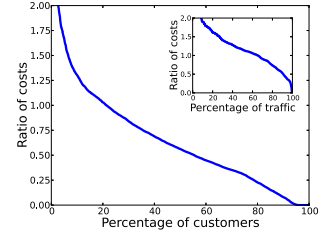
(a) Volume–device policy



(b) Customer peak–device policy

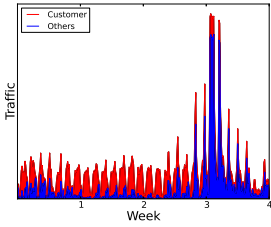


(c) 95th percentile–device policy

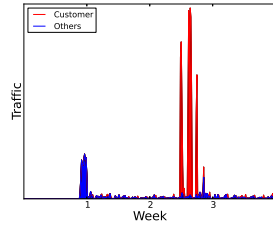


(d) Aggregate peak–device policy

Fig. 4. Discrepancies between the cost sharing policies and the Shapley costs; distribution of their ratios



(a) Volume–device policy



(b) Aggregate peak–device policy

Fig. 5. Traffic pattern of single customers with the largest maximal discrepancies given non-negligible traffic volumes

customer causes a high cost for the given link (figure not shown). Despite the customer’s modest aggregate volume, these peaks result in the large discrepancy of this policy, whereas the real marginal contribution of the customer to the overall cost of the device is limited.

95th percentile–device policy: The customer has on the one hand non-negligible 95th percentile traffic while on the other hand it barely contributes to the real cost of the link (figure not shown).

Aggregate peak–device policy: The customer is almost exclusively responsible for the peak utilization of the link (Fig. 5(b)); thus, the policy allocates nearly all the costs to it. However, the other customers have a substantial contribution during the other peaks on the link, thus their marginal contribution to the total cost is not negligible. Accordingly, the Shapley–device policy allocates more cost to the other customers and hence fewer costs to the analyzed customer.

Based on the presented empirical results, we identified several discrepancies of the cost sharing policies. However, there are additional factors that contribute to the complexity of estimating the costs of customers in backbone networks. Next,

we highlight two of them by focusing on how the geographic location of the network devices impacts the costs of customers and on the impact of the granularity of the metering.

B. Impact of geographic location

As we illustrated in the third and fourth case of the toy example, the different cost functions across geographic locations affect the costs of the customers. We show the aggregate relative costs of the largest customers in Fig. 3(b) where we consider the geographically diverse cost structure. The impact of geography is threefold. First, the cost of the customers increases because the costs of the links are higher in Europe and Latin America than the USA costs we used earlier. Second, the location-based costs alter the difference between the costs of specific customers. Finally, the location of the links affects the cost-based rank of the customers.

C. The impact of metering

As we highlighted in the introduction, there exists a trade-off between accuracy and the resources used to monitor the traffic. Analogously to the second and third case of the toy example, we illustrate this by comparing the costs of customers in two metering scenarios. In the first case, we monitor the traffic volumes of the customers on every link as we did before. We aggregate the traffic of customers into a single link in the second case and we share the cost of the whole infrastructure based on this unique time-series. In Fig. 3(c) we present the distribution of the ratio between the 95th percentile–device and the 95th percentile–customer policies. A significant portion of the customers face high discrepancies due to the different resolution of the metering. The costs diverge by at least 25% in 41.7% of the cases while the disparity of the costs is as high as $\times 10$ in 12.5% of the customers.

IV. RELATED WORK

We refer to the textbook of Courcoubetis and Weber [7] for a thorough treatment of pricing in communication networks.

Several studies investigated how to reduce the transit costs including ISP peering [2, 8, 9], CDNs [19], P2P localization [6], and traffic smoothing [17]. Dimitropoulos et al. [10] presented a comprehensive analysis of the 95th percentile pricing. A proposal by Laoutaris et al. [13, 12] showed how traffic can be transferred in the network without increasing the 95th percentile of the customers. A recent proposal by Stanojevic et al. [23] proposes to the customers of transit providers to form a coalition to reduce their transit costs. Valancius et al. [25] propose to price the traffic of backbone networks based on a few pricing tiers. Due to the presented discrepancies, our empirical results suggest that a tiered pricing may not be precise and fair as multiple factors have significant impact on the costs of the customers.

Due to the desirable fairness properties [1, 11, 18] of the Shapley value [21], recent studies proposed pricing and cost sharing mechanisms using Shapley values. Briscoe [4, 5] motivates the usage of mechanisms that share the costs of the users fairly. Cooperative approaches for cost sharing are investigated in case of inter-domain routing [16, 22] and IP multicast [1, 11]. Ma et al. [14, 15] presented a fair revenue sharing method for ISPs that quantifies the importance of each ISP in the Internet ecosystem. The work of Stanojevic et al. [24] is the closest to ours. The authors empirically investigated the temporal usage effects using the Shapley value and the 95th percentile method. Our work is different in several ways: a) we focus on the costs of the large customers of a backbone network with geographically diverse links; b) we study three additional alternative cost sharing policies; and c) we apply a more realistic stepwise cost function.

V. CONCLUSION

By presenting several discrepancies of the cost sharing policies we illustrated that quantifying the real costs of network flows—and thus pricing them—is a highly challenging and complex issue. Despite the computational complexity of the Shapley–device policy, this method better reflects the costs of the customers. Although customers may find the other policies straightforward and easier to understand, the costs yielded by these policies are disconnected from the actual costs in a significant number of cases. We showed that the application of volume based, 95th-percentile-based and other pricing policies is not suitable neither for the network operators nor for the customers due to their lack of monetary fairness. As future work, we plan to extend our investigation into an additional level of network metering, *i.e.*, include the costs and traffic characteristics of the devices located inside the backbone network.

ACKNOWLEDGEMENT

We would like to thank Jose Ignacio Cristobal Regidor, Elena Sanchez Carretero, Juan Manuel Ortigosa, Emilio Sepulveda, Jose Pizarro, and Antonio Santos Sanchez from Telefonica for their valuable insights. This work and its dissemination

efforts have been supported in part by the ENVISION FP7 project of the European Union.

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